# Full Feedforward of Grid Voltage for Grid-Connected Inverter With *LCL* Filter to Suppress Current Distortion Due to Grid Voltage Harmonics

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Abstract—The grid-connected inverter with an LCL filter has the ability of attenuating the high-frequency current harmonics. However, the current distortion caused by harmonics in the grid voltage is difficult to be eliminated. Increasing the loop gain can reduce the current distortion, but this approach is compromised by the system stability requirement. Without increasing the loop gain, applying feedforward of the grid voltage can suppress the effect of grid voltage harmonics. This paper proposes the feedforward function of the grid voltage for the grid-connected inverter with an *LCL* filter. Specifically, the proposed feedforward function involves proportional, derivative, and second derivative of the grid voltage, and can be simplified according to the dominant harmonics in the grid voltage. The proposed feedforward scheme can effectively suppress the current distortion arising from the grid voltage harmonics, and the steady-state error of the injected current can be substantially reduced even if a conventional proportional and integral regulator is applied. A 6-kW experimental prototype has been tested to verify the effectiveness of the proposed feedforward scheme.

Index Terms—Damping resonance, dual-loop control, feedforward, LCL filter, total harmonic distortions (THD).

#### I. INTRODUCTION

In the past decade, the increasing demand of energy and the pressing need for reduction of greenhouse gas emission have prompted a renewed interest in the use of renewable energy, such as wind energy, microhydroenergy, and solar energy, which are rapidly increasing their share in distributed generation (DG) [1]. Unlike conventional centralized generators, these DG systems form decentralized subnetworks, providing improved power quality and reliability. However, the requirement for safe and smart operation of DG subnetworks has posed new challenges to the design of the related power electronics systems as well as the design of the subnetworks themselves (i.e., microgrids) [2]–[6]. In practice, DG subnetworks or microgrids are

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normally connected to the power grid through grid-connected inverters, which play an important role in ensuring high-quality power to be injected into the power grid. In the grid-connected inverter, an inductor is usually used as an interface between the inverter and the grid. However, if only an inductor is used, high-frequency switching is needed to ensure that no excessive harmonics are generated from pulsewidth modulation (PWM), but this would be accompanied by the undesirable problems of switching losses and electromagnetic interference (EMI), especially for high power applications [7].

The use of an *LCL* filter in lieu of a single inductor is an effective alternative for attenuating the current harmonics caused by PWM, since the additional capacitor branch can bypass the high-frequency harmonics. However, the frequency response of an *LCL* filter has a resonance peak, and presents zero impedance to the harmonics at the resonant frequency from the inverter or the grid. If an improper controller is used, the inverter may become unstable [8], [9].

To damp the resonance, an additional resistor can be inserted in series with the filter capacitor. This passive damping solution is very simple and highly reliable. However, the additional resistor results in power loss and weakens the attenuation ability of the LCL filter [10], [11]. This drawback can be overcome by employing active damping [12]–[14]. Blasko and Kaura [13] controlled the filter capacitor voltage via a lead-lag regulator to damp the resonance. The additional compensator introduces a negative resonance peak to compensate the positive resonance peak of the LCL filter. A similar approach based on applying feedback of the capacitor current to damp the resonance was proposed by Twining and Holmes [14]. Liserre et al. [15], [16] used a second-order or fourth-order digital filter to compensate the resonance peak. However, the compensation ability of the digital filter is highly dependent on the parameters of the LCL filter. An interesting control strategy based on the feedback of the splitting capacitor current was proposed by Shen et al. [11]. With this method, the injected current is not controlled directly, and the damping ability is also highly dependent upon the parameters of the LCL filter. Among all these active damping solutions, the solution involving feedback of the capacitor current has attracted considerable attention [14], [17].

Besides the problem associated with resonance of the *LCL* filter, the harmonics in the grid voltage is another issue in the design of grid-connected inverter. Proportional resonance (PR) regulator can provide infinite gain at the selected resonant frequency to suppress the effect of the unwanted harmonics [18]–[20]. The main disadvantage of PR regulator is that it will

reduce the system's phase margin if the harmonics to be removed is in the proximity of the crossover frequency of the loop gain [15]. Another method for suppressing current harmonics is to incorporate the variation of the grid voltage in the control through an additional feedforward path [21], [22]. The basic idea is to increase the output impedance of the grid-connected inverter, further enhancing the suppression ability. In comparison with PR regulator, this approach does not affect the phase margin. However, recent attempts in realizing this approach have only succeeded in partial feedforwarding of the grid voltage. Obviously, the suppression ability is not satisfactory.

This paper studies the feedforward scheme for grid-connected inverter with an LCL filter. Section II analyzes the dual-loop control strategy based on the feedback of the capacitor and the injected current, and derives a simplified mathematical model for the grid-connected inverter with an LCL filter based on the control strategy through a series of equivalent transformations. Based on the simplified model, Section III investigates the application of the feedforward scheme for eliminating the effect of harmonics in the grid voltage. Using the simplified block diagram, a full feedforward of the grid voltage is proposed in Section IV. The design procedure of the dual-loop controller of the proposed control strategy is presented in Section V. In order to verify the effectiveness of the proposed feedforward scheme, a 6-kW experimental prototype is built and tested. Specifically, experimental waveforms are presented in Section VI. Finally, Section VII concludes this paper.

# II. SYSTEM CONFIGURATION AND AVERAGE SWITCHING MODEL

Fig. 1(a) shows the configuration of a single-phase grid-connected inverter with an LCL filter. Here, the LCL filter is composed of  $L_1$ , C, and  $L_2$ . Fig. 1(b) shows the average switching model of the inverter with an LCL filter, where  $v_M(s)$  is the modulating signal, and  $G_{\text{inv}}(s)$  is the gain of PWM inverter [11], [14], which is expressed as follows:

$$G_{\rm inv}\left(s\right) = \frac{V_{\rm in}}{V_{\rm tri}} \tag{1}$$

where  $V_{\rm in}$  is the input dc voltage and  $V_{\rm tri}$  is the amplitude of the carrier.

We define  $Z_{L_1}(s)$ ,  $Z_C(s)$ , and  $Z_{L_2}(s)$  as the impedances of  $L_1$ , C, and  $L_2$ , respectively, which are expressed as follows:

$$Z_{L_1}(s) = sL_1 \tag{2}$$

$$Z_C(s) = \frac{1}{sC} \tag{3}$$

$$Z_{L_2}(s) = sL_2. (4)$$

Here, the equivalent series resistors of  $L_1$ , C, and  $L_2$  are relatively small and can be ignored.

# III. DUAL-LOOP CONTROL STRATEGY

The primary objective of the control strategy for the gridconnected inverter is to control the current that is injected into the grid, so that it follows the grid voltage in phase and its am-

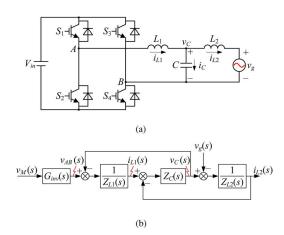


Fig. 1. Single-phase grid-connected inverter with *LCL* filter. (a) Circuit topology. (b) Block diagram of average switching model.

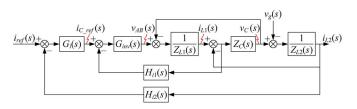


Fig. 2. Block diagram of dual-loop control strategy based on the feedback of capacitor current and injected current.

plitude can be regulated as required. Due to the resonance of the LCL filter, a single current loop is not adequate to ensure stability of the system. Thus, an inner loop incorporating feedback of the capacitor current is usually employed [14], [17], [23]. By cascading the inner loop with the outer loop, which is the injected current loop, a dual-loop control strategy is constructed. Fig. 2 shows the block diagram of the control strategy, where  $i_{\rm ref}(s)$  is the injected current reference of the outer loop,  $H_{i1}(s)$  and  $H_{i2}(s)$  are sensor gains of the filter capacitor current and injected current, respectively, and  $G_i(s)$  is the transfer function of the outer loop.

As shown in Fig. 2, the inner loop is interacting with the thirdorder LCL filter, implying that the design of the two regulating loops can be quite complicated. To simplify the design procedure, an equivalent model containing decoupled regulating loops would be desirable. A series of equivalent transformations of the system in terms of block diagrams is shown in Fig. 3, where the dash lines represent the original status, and the bold solid lines represent the destination status. First, replacing the feedback signal  $v_C(s)$  with  $i_C(s)$ , and relocating its feedback node to the output of  $G_i(s)$ , an equivalent block diagram is obtained, as shown in Fig. 3(a). Second, by combining the two feedback functions of the input signal of the transfer function  $Z_C(s)$ , and moving the inner feedback node of  $i_{L_2}(s)$  from the output of the transfer function  $1/Z_{L_1}(s)$  to the output of the transfer function  $G_i(s)$ , the equivalent block diagram is obtained, as shown in Fig. 3(b). Third, moving the inner feedback node of  $i_{L_2}(s)$  from the output of the transfer function  $G_i(s)$  to the output of the transfer function  $Z_C(s)$ , and then, simplifying the forward path from the transfer function  $G_i(s)$  to the transfer function  $Z_C(s)$ ,

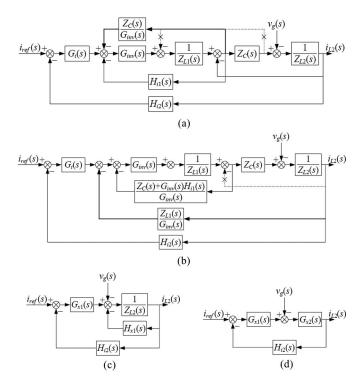


Fig. 3. Equivalent transformation of block diagram of the dual-loop control strategy.

results in the equivalent block diagram shown in Fig. 3, where

$$G_{x1} = \frac{G_i G_{\text{inv}} Z_C}{Z_{L_1} + Z_C + H_{i1} G_{\text{inv}}}$$
 (5)

$$H_{x1} = \frac{Z_{L_1} Z_C}{Z_{L_1} + Z_C + H_{i1} G_{inv}}.$$
 (6)

Furthermore, Fig. 3(c) can be simplified to Fig. 3(d), where

$$G_{x2} = \frac{Z_{L_1} + Z_C + H_{i1}G_{\text{inv}}}{Z_{L_1}Z_{L_2} + (Z_{L_1} + Z_{L_2})Z_C + H_{i1}G_{\text{inv}}Z_{L_2}}.$$
 (7)

From Fig. 3(d), the loop gain T can be obtained as follows:

$$T = G_{x1}G_{x2}H_{i2}$$

$$= \frac{G_iG_{\text{inv}}Z_CH_{i2}}{Z_{L_1}Z_{L_2} + (Z_{L_1} + Z_{L_2})Z_C + H_{i1}G_{\text{inv}}Z_{L_2}}$$
(8)

and the relationship between the inputs and output can be expressed as follows:

$$i_{L_2} = \frac{T}{1+T} \frac{1}{H_{i2}} i_{\text{ref}} - \frac{G_{x2}}{1+T} v_g.$$
 (9)

From (9), we see that the steady-state error of  $i_{L_2}$  is caused by the usual static tracking error as well as variation resulting from  $v_g$ . Here, the static tracking error is a function of the current reference  $i_{\rm ref}$ . From (7) and (9), it can be seen that if the outer loop gain  $G_i$  is large enough in magnitude, both the static tracking error and the variation resulting from  $v_g$  will be substantially reduced. However, if a conventional regulator, such as proportional—integral (PI) regulator is employed, only the static tracking error can be substantially reduced, while the variation resulting from  $v_g$  may become significant.

### IV. APPLICATION OF FEEDFORWARD OF THE GRID VOLTAGE

Besides increasing the gain of the outer loop regulator  $G_i$ , application of feedforward of the grid voltage can also suppress the effect of  $v_g$  [22]. In (9), the function  $-G_{x2}/(1+T)$  can be regarded as the admittance between  $v_g$  and  $i_{L_2}$ . If an additional path is introduced, as shown in Fig. 4(a), the effect of  $v_g$  will be eliminated. By moving the feedforward node from the output of  $G_{x2}(s)$  to the output of  $G_{x1}(s)$ , and modifying the feedforward function as appropriate, the equivalent block diagram can be obtained, as shown in Fig. 4(b). Fig. 4(b) can be further transformed, as shown in Fig. 4(c). It can be seen from Fig. 4(c) that feedforward of  $v_g$  with the function of  $1/G_{x1}(s)$  will eliminate the effect of  $v_g$  on the injected current  $i_{L_2}$ .

From Fig. 4(c), we can reconfigure the block diagram of Fig. 2, as shown in Fig. 5(a). Note that the numerator of  $G_{x1}(s)$ , as shown in (5), includes the function  $G_i(s)$ . Thus, Fig. 5(a) can be equivalently transformed into Fig. 5(b), where the feedforward component contributes to the modulation of the duty cycle.

The feedforward function in Fig. 5(b) can be expressed as follows:

$$\frac{G_i}{G_{x1}} = \frac{1}{G_{\text{inv}}} \left( 1 + \frac{Z_{L_1}}{Z_C} + \frac{H_{i1}G_{\text{inv}}}{Z_C} \right). \tag{10}$$

Clearly, from (10), it can be seen that in order to eliminate the effect of  $v_g$ , three components are needed. Thus, if only  $1/G_{\rm inv}(s)$  is used, as attempted previously in [22], the result will not be very satisfactory.

Putting the three feedforward components indicated in (10) into the feedforward function in Fig. 5(b), the equivalent transformation is obtained, as shown in Fig. 6. It can be seen that one of the feedforward functions is proportional feedforward of  $v_g$ , and the other two feedforward functions are related to the impedance of the LCL filter. Based on (2) and (3), the other two feedforward functions are as follows:

$$\frac{H_{i1}}{Z_C} = sCH_{i1} \tag{11}$$

$$\frac{Z_{L_1}}{G_{\text{inv}}Z_C} = s^2 \frac{L_1 C}{G_{\text{inv}}} \tag{12}$$

which are the derivative and second-derivative feedforward functions of  $v_g$ , respectively.

The implementation of the proposed control strategy is shown in Fig. 7, where  $i_{\rm ref}$  is the reference of the injected current to the grid, and  $H_v$  is the feedback coefficient of  $v_g$ . In order to ensure a high-quality current injected to the grid,  $i_{\rm ref}$  should be controlled appropriately. In practice, the waveform of the injected current is controlled to follow a sine wave by means of table look-up using a DSP, and its phase is locked by a phase-locked loop (PLL) algorithm.

The feedforward function  $G_{\rm fd}(s)$  shown in Fig. 7 is given by

$$G_{\rm fd} = \frac{1 + sCH_{i1}G_{\rm inv} + s^2L_1C}{G_{\rm inv}H_v}.$$
 (13)

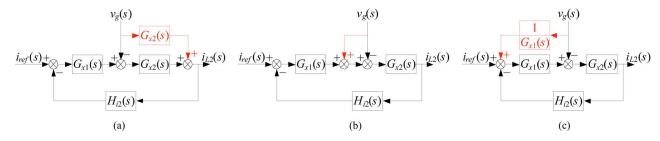


Fig. 4. Block diagram of feedforward scheme and its equivalent transforms.

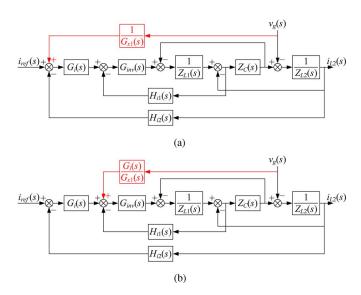


Fig. 5. Block diagrams of feedforward scheme and equivalent representations.

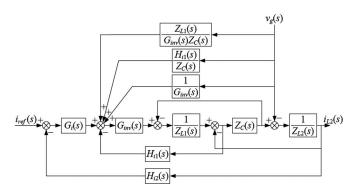


Fig. 6. Block diagrams of dual-loop control strategy with full feedforward of grid voltage.

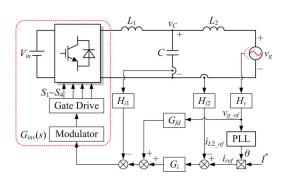


Fig. 7. Schematics diagram of the grid-connected inverter.

TABLE I PARAMETERS OF THE PROTOTYPE

Parameter	Value	Parameter	Value
$V_{ m in}$	360 V	$L_1$	600 μΗ
$V_g$ (rms value)	220 V	C	$10  \mu \mathrm{F}$
$f_{ m grid}$	50 Hz	$L_2$	200 μΗ
$P_o$	6 kW	$H_{i1}$	0.075
$f_s$	10 kHz	$H_{i2}$	0.15

# V. DESIGN PROCEDURES

# A. Prototype Construction

A 6-kW prototype has been constructed to verify the proposed feedforward scheme. The parameters of the prototype are given in Table I. The controller employs carrier phase shift (CPS) sinusoidal pulsewidth modulation (SPWM).

Comparison of Figs. 2 and Fig. 6 shows that the loop gain T is not changed after the application of feedforward of  $v_g$ . Therefore, the parameters of the regulators corresponding to Figs. 2 and Fig. 6 should be the same if the stability margin is uniform. The following design is based on the dual-loop control strategy shown in Fig. 2. The inner loop will be designed first and followed by the design of the outer loop.

# B. Inner Loop Design

The main objective of the inner loop is to damp the resonance. When the outer loop is uncompensated, i.e.,  $G_i(s)$  is 1, the loop gain expressed in (8) is as follows:

$$T_u = \frac{G_{\text{inv}} Z_C H_{i2}}{Z_{L_1} Z_{L_2} + (Z_{L_1} + Z_{L_2}) Z_C + H_{i1} G_{\text{inv}} Z_{L_2}}.$$
 (14)

With the carrier amplitude  $V_{\rm tri}$  is equal to 3 V, the inverter transfer function  $G_{\rm inv}(s)$  has a magnitude of 120 according to (1). In the implementation,  $V_{\rm tri}$  is converted from a digital modulator to an analog modulator. Using the parameters in Table I, according to (14), the Bode diagrams are depicted, as shown in Fig. 8. The dashed line shows the Bode diagram without the inner loop, i.e.  $H_{i1}(s)$  is 0, and it can be seen that the amplitude of the loop gain has a large resonant spike. When the inner loop is added, where  $H_{i1}(s)$  is 0.075, the resonant spike is effectively damped, as shown in the solid lines.

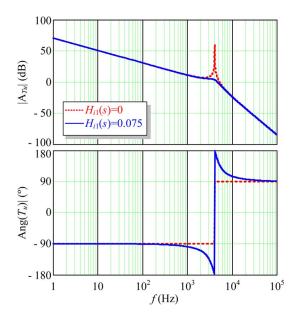


Fig. 8. Bode diagram of loop gain for inner loop design.

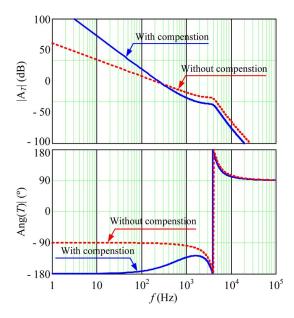


Fig. 9. Bode diagram of loop gain for outer loop design.

# C. Outer Loop Design

After designing the inner loop, the parameters of the outer loop can be easily designed. Since the task of the outer loop is to reduce the steady-state error, a PI regulator can be used. When the sensor gain  $H_{i2}(s)$  is set to 0.15 and the regulator  $G_i(s)$  is 0.4 + 1700/s, the Bode diagram is shown in Fig. 9. Here, the cross frequency is about 2 kHz, the amplitude margin is about 4 dB, and the phase margin is about 45°. The gain at 50 Hz is about 50 dB, which means that the disturbance can be attenuated by a factor of 0.01. Obviously, the stability margin is satisfactory and the steady-state error is acceptable.

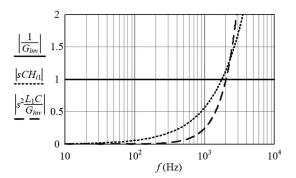


Fig. 10. Comparison of the three feedforward components.

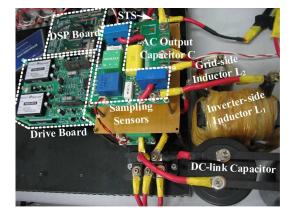


Fig. 11. Photograph of the single-phase grid-connected inverter prototype.

#### D. Discussion of the Three FeedForward Components

After completing the design of the dual loops, all the parameters of the grid-connected inverter are fixed, including the coefficients of the three feedforward functions. The proportional feedforward coefficient is  $8.3 \times 10^{-3}$ , which is the reciprocal of  $G_{\rm inv}(s)$  as defined in (10). Also, as defined in (11) and (12), the derivative and second-derivative feedforward coefficients can be calculated, as shown in Fig. 10. Note that the three feedforward components are expressed in percent unit values. From Fig. 10, we can see that the derivative feedforward coefficient is an order of magnitude smaller than the proportional feedforward coefficient when  $v_a$  contains only third harmonic distortion, and that the second-derivative feedforward coefficient is also an order of magnitude smaller than the proportional feedforward coefficient when  $v_q$  contains harmonic distortion up to the 13th harmonic. This means that the second-derivative feedforward function can be omitted if  $v_q$  contains harmonic distortion within the 13th harmonic, and only the proportional feedforward coefficient is needed if  $v_q$  contains only the third harmonic.

#### VI. EXPERIMENTAL RESULTS

### A. Experimental Setup

A 6-kW prototype, as shown in Fig. 11, was constructed for verification of the full-feedforward scheme and for comparing the effectiveness of the three constituent feedforward functions. The single-phase grid-connected inverter was

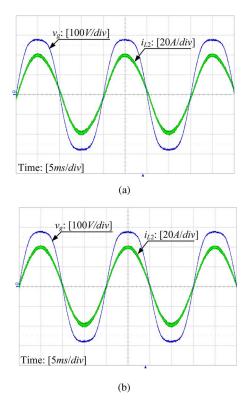


Fig. 12. Experimental waveforms of two control strategies. (a) Case I. (b) Case II.

implemented using two insulated gate bipolar transistor modules (DM2G100SH12AE). These modules are driven by M57962 L. The grid voltage  $v_g$ , which was used in the PLL, was sensed by a voltage hall (LV28-P). The capacitor current was indirectly sensed through the difference of  $i_{L_1}$  and  $i_{L_2}$ , which were measured by two current halls (LA55-P). The dual regulators were implemented by a high-speed DSP (TMS320F2812). An extended 14-bit A/D converter (MAXIM-1324ECM) was used.

In translating to the z-domain, we put  $s = (1 - z^{-1})/T$  to obtain the backward difference equation for the outer loop gain, i.e.,

$$G_i(z) = k_p + \frac{k_i T_s}{1 - z^{-1}}$$
 (15)

where  $k_p$  and  $k_i$  are the proportional and integral coefficients, and  $T_s$  is the sampling period. Likewise, the feedforward function is given in (16) as shown at the bottom of this page.

The sampling action is taken at the bottom and top of the carrier signal. In our experiment,  $T_s$  is set to 50  $\mu$ s. Since the computational delay is about 2.1  $\mu$ s, which is very small compared to the sampling period, the computation required by the full feedforward of  $v_g$  can be completed within a sampling period. It should be noted that a digital low-pass filter (LPF) might be needed for noise attenuation in some cases. In our case, how-

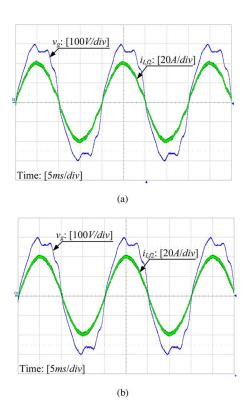


Fig. 13. Experimental waveforms of two feedforward control strategies. (a) Case II. (b) Case III.

ever, the use of a LPF with corner frequency of 10 kHz has been tested and found unnecessary.

# B. Results

Referring to the design procedure developed in Section V, experimental results of four cases are compared. Case I is the dual-loop strategy without feedforward of  $v_g$ , as shown in Fig. 2. Case II is the dual-loop strategy with proportional feedforward of  $v_g$ , i.e., only  $1/G_{\rm inv}(s)$  is used as the feedforward function. Case III is the dual-loop strategy with proportional and derivative feedforward of  $v_g$ . Case IV is the dual-loop strategy with full feedforward of  $v_g$ , i.e., proportional, derivative, and second-derivative feedforward of  $v_g$  are all used.

We use a programmable ac source (Chroma 6590) to simulate the grid voltage. Fig. 12 shows the experimental results for Cases I and II at full-load condition. Here, the third harmonic has been injected into  $v_g$ , and the magnitude and phase of the injected harmonic is 10% and  $0^\circ$ , respectively, with respect to the fundamental component. It can be seen that the waveforms of  $i_{L_2}$  is distorted in Case I, and a phase difference of about  $4.4^\circ$  exists between  $i_{L_2}$  and  $v_g$ . It can be seen from the analysis in Section III that the phase lag is resulted from the fundamental component of  $v_g$ . Based on the parameters in Table I, the phase lag between  $i_{L_2}$  and  $v_g$  can be calculated to be  $4.8^\circ$ , which is

$$G_{\rm fd}(z) = \frac{\left(T_s^2 + CH_{i1}G_{\rm inv}T_s + L_1C\right) - \left(CH_{i1}G_{\rm inv}T_s + 2L_1C\right)z^{-1} + L_1Cz^{-2}}{G_{\rm inv}H_vT_s^2}.$$
(16)

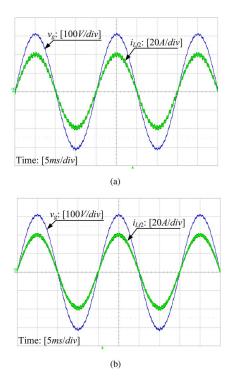


Fig. 14. Experimental waveforms of two feedforward control strategies. (a) Case III. (b) Case IV.

very close to the experimental result. For Case II, as shown in Fig. 12(b),  $i_{L_2}$  is perfectly sinusoidal, and the phase lag has been eliminated. The total harmonic distortions (THDs) of the waveforms of  $i_{L_2}$  shown in Fig. 12(a) and Fig. 12(b) are 3.21% and 1.2%, respectively. The results show that when the distortion contains only third harmonic, the proportional feedforward scheme (Case II) is effective in suppressing the distortion.

Fig. 13 shows the experimental results for Cases II and III at full-load condition. Here, the injected harmonics into  $v_g$  include the 3rd, 5h, 7th, 9th, 11th, and 13th harmonics, and the magnitudes of the injected harmonics with respect to the fundamental component of  $v_g$  are 10%, 5%, 3%, 3%, 2%, and 2%, respectively, and the corresponding phase angles are  $0^{\circ}$ ,  $90^{\circ}$ ,  $0^{\circ}$ ,  $0^{\circ}$ ,  $0^{\circ}$ , and  $0^{\circ}$ . The measured THDs of the waveforms of  $i_{L_2}$  shown in Fig. 13(a) and Fig. 13(b) are 2.61% and 1.42%, respectively. The results show that when the distortion is limited to harmonics up to the 13th harmonic, the proportional and derivative feedforward scheme (Case III) is effective in suppressing the distortion, while the proportional feedforward scheme (Case II) is inadequate.

Fig. 14 shows the experimental results for Case III and Case IV at full-load condition. Here, 33rd harmonic, with magnitude and phase of 1% and 0° with respect to the fundamental, has been injected into  $v_g$ . The measured THDs of  $i_{L_2}$  for Cases III and IV are 2.45% and 1.31%, respectively. The results show that when the distortion contains higher harmonics, the full-feedforward scheme is necessary for eliminating the distortion.

Furthermore, we conducted a test to verify the effectiveness of the proposed scheme under possible voltage dip conditions. Fig. 15 shows the experimental results for the four cases when

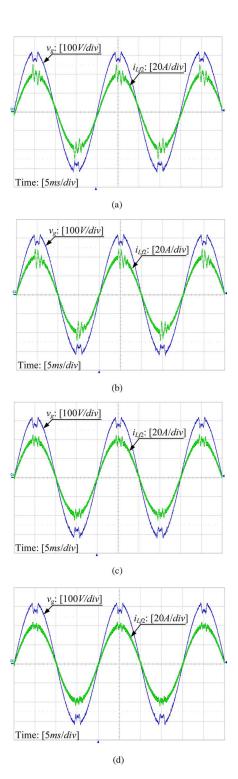


Fig. 15. Experimental waveforms for the four control strategies under voltage dip conditions. (a) Case I. (b) Case II. (c) Case III. (d) Case IV.

a 40 V voltage dip occurs at the trough and crest of the voltage waveform of  $v_g$ . The THDs of  $i_{L_2}$  for the four cases are 4.61%, 5.42%, 3.26%, and 2.24%, respectively. The results show that the full-feedforward scheme can effectively suppress the current distortion even  $v_g$  experiences a voltage dip.

The transient response of the grid-connected inverter under the proposed full-feedforward control has been studied, and the

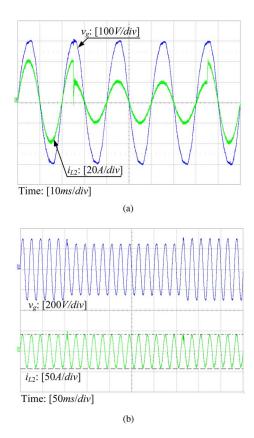


Fig. 16. Measured transient response under (a) step change in  $i_{\rm ref}$  and (b) step change in  $v_q$  .

results are shown in Fig. 16(a) corresponding to step change of  $i_{\rm ref}$ . Note that the grid voltage is taken from the real power grid. Here,  $i_{\rm ref}$  is stepped up from half load to full load, and *vice versa*. The load changes are intentionally set to occur at the peak of  $i_{L_2}$ , which is the worst case. The results show that  $i_{L_2}$  is still kept in phase with  $v_g$ , with small oscillatory transient observed immediately after the step change of  $i_{\rm ref}$ . Also, Fig. 16(b) shows the transient response corresponding to step change of  $v_g$  with the full-feedforward scheme. Here,  $v_g$  is stepped down from 220 to 180 V, and *vice versa*. The  $v_g$  changes are again purposely set to occur at the peak of  $v_g$ , which is the worst case. Results show that the amplitude of  $i_{L_2}$  is kept unchanged, with small oscillatory transient immediately following the step change of  $v_g$ .

#### VII. CONCLUSION

For the grid-connected inverter with an *LCL* filter, the dual-loop control strategy with feedback of the capacitor and the injected current can damp the resonance effectively, but it cannot attenuate the current distortion resulted from the harmonics in the grid voltage. The traditional solution of applying a feedforward grid voltage can suppress such current distortion, but the result is not satisfactory, especially when the order of the harmonics is high. This paper proposes a full feedforward of grid voltage scheme to suppress the injected current distortion arising from harmonics in the grid voltage. Four cases of control schemes, namely, dual-loop control strategy without feedforward, dual-loop strategy with proportional feedforward

of the grid voltage, dual-loop strategy with proportional and derivative feedforward of the grid voltage, and dual-loop strategy with full feedforward of the grid voltage, are compared. Some design guidelines are recommended. Our results show that if the grid voltage contains only the third harmonic, proportional feedforward of the grid voltage is adequate for achieving good suppression of the current distortion. If the grid voltage contains harmonic distortion up to 13th harmonic, proportional and derivative feedforward of the grid voltage is adequate for achieving good suppression of the current distortion. If the grid voltage contains higher harmonic distortion, the full feedforward of the grid voltage becomes necessary. Furthermore, the proposed feedforward scheme has an added merit that it is able to reduce the steady-state error of the injected current significantly even if simple conventional PI regulation is used. The injected current can thus accurately track the reference current for most practical applications.

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